

SITE NUMBER—07144100**SITE NAME**—Little Arkansas River near Sedgwick**DATE CREATED**—3/15/2013**MODEL DEVELOPMENT DATA PERIOD**—5/1/1998 – 9/22/2011

MODEL-CALIBRATION DATASET—All data were collected using U.S. Geological Survey (USGS) protocols and are stored in National Water Information System (NWIS) database. The regression model is based on 158 concurrent measurements of specific conductance, streamflow, and alkalinity samples collected from 05-01-1998 through 09-22-2011. Samples were collected throughout the range of continuously observed hydrologic flow rate and specific conductance conditions. Specific conductance and streamflow values are time-averaged, approved unit values corresponding with the duration of sample collection. Summary statistics and complete model-calibration dataset are provided. A single alkalinity value was deemed an outlier.

Outlier removed from the dataset.

Date	Specific conductance, in microsiemens per centimeter at 25 degrees Celsius	Streamflow, in cubic feet per second	Alkalinity, in milligrams per liter as calcium carbonate
7/10/1998	211	1,360	18

The documentation to review the alkalinity analysis was unavailable. However, the alkalinity value was 10 times less than the minimum alkalinity at similar specific conductance and streamflow values. For this reason, the sample was removed from the dataset.

MODEL DEVELOPMENT—Regression analysis was done using S-PLUS, R, and a spreadsheet macro that examined specific conductance and streamflow together as explanatory variables for estimating alkalinity. Different combinations of untransformed and \log_{10} -transformed data were evaluated. Alkalinity, specific conductance and streamflow were selected as the best model based on residual plots, model standard percentage error (*MSPE*), adjusted R^2 , prediction error sum of squares (*PRESS*), and Mallow's C_p . Model spreadsheet is archived and can be found at <http://nrtwq.usgs.gov/ks> for review, and contains all relevant sample data and more in-depth statistical information.

MODEL SUMMARY—Summary of final regression analysis for alkalinity concentration at site number 07144100.

Specific conductance and streamflow-based model:

$$\log_{10}(Alk) = 0.731 \times \log_{10}(SC) - 0.1 \times \log_{10}(Q) + 0.381 ,$$

where

Alk = alkalinity, in milligrams per liter as calcium carbonate;

SC = specific conductance, in microsiemens per centimeter at 25 degrees Celsius; and

Q = streamflow, in cubic feet per second.

The use of specific conductance and streamflow as explanatory variables makes sense both physically and statistically. Physically because alkalinity is composed of major ions that affect the conductivity of water and results in a clear correlation between alkalinity and specific conductance. Alkalinity correlates well with streamflow because high streamflow values tend to dilute concentrations of dissolved constituents associated with alkalinity. Specific conductance and streamflow make statistical sense as explanatory variables because they resulted in a model with low Mallow's C_p and PRESS values, and high adjusted R^2 values.

ALKALINITY RECORD— The record is computed using the regression model in the National Real-Time Water Quality (NRTWQ) website. Data are computed at hourly intervals. The record is complete for the year except as noted. The specific conductance monitor was removed during winter months because of below freezing conditions. A more in-depth description of the water quality record can be found at – <http://nrtwq.usgs.gov/ks>.

REMARKS—

- Site location, equipment, and other stream-gaging station information can be found in the Site Information Management System (SIMS).

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Reviewed: Pat Rasmussen

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Model Form

$$\log(\text{Alk}) = 0.731 * \log(\text{SC}) - 0.1 * \log(\text{Q}) + 0.381$$

Explanatory variable summary statistics

	<u>log(SC)</u>	<u>SC</u>	<u>log(Q)</u>	<u>Q</u>
Minimum	1.732	54.0	0.4940	3.12
1st Quartile	2.441	276	1.698	49.9
Median	2.765	582	2.225	168
Mean	2.675	585	2.409	1460
3rd Quartile	2.941	871	3.144	1400
Maximum	3.126	1340	4.181	15200

Notes:

Dependent variable summary statistics

	<u>log(Alk)</u>	<u>Alk</u>
Minimum	1.301	20.0
1st Quartile	1.810	64.5
Median	2.137	137
Mean	2.094	155
3rd Quartile	2.396	249
Maximum	2.502	318

Notes:

Model Calibration

Basic Data

Number of Measurements:	158
Standard Error:	0.0646
MSPE (Upper)	+16.05
MSPE (Lower)	-13.83
R ²	0.96
Adj R ²	0.96
Duan BCF:	1.01
VIF	3.51

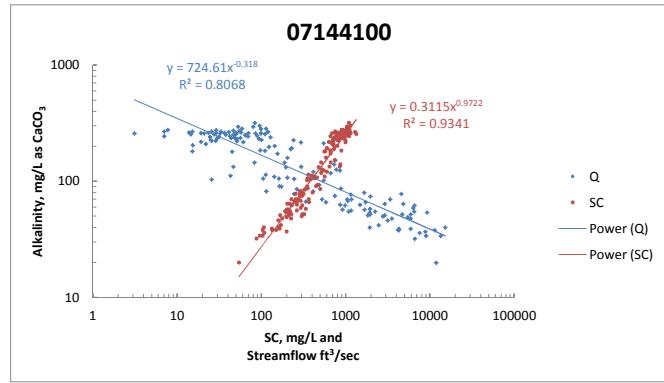
Explanatory Variables

<u>Variable</u>	<u>Value</u>	<u>Standard Error</u>
Intercept	0.381	0.1075
$\log(\text{SC})$	0.731	0.0314
$\log(\text{Q})$	-0.1	0.0110

Notes:

Covariance Matrix

	<u>Intercept</u>	<u>log(SC)</u>	<u>log(Q)</u>
Intercept	1	-0.99	-0.908
$\log(\text{SC})$	-0.99	1	0.846
$\log(\text{Q})$	-0.908	0.846	1



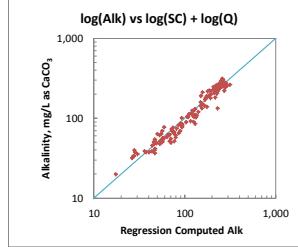
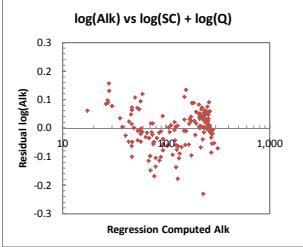
Test Criteria

<u>Leverage</u>	<u>Cook's D</u>	<u>DFITS</u>
0.0570	0.843	0.276

Observations exceeding at least one test criterion

<u>Observation</u>	<u>Observed</u>	<u>Standardized</u>
1	2.15	2.24
4	1.72	1.88
13	1.51	1.42
19	1.72	1.83
35	1.89	1.77
51	1.53	1.43
93	1.30	1.24
99	2.41	2.41
113	1.70	1.85
134	2.33	2.19
140	1.58	1.45
141	1.60	1.44
156	2.13	2.35
157	2.02	2.13

Notes:



<u>Date</u>	<u>SC, µS/cm</u>	<u>Streamflow, ft³/sec</u>	<u>Alkalinity, mg/L as CaCO₃</u>	<u>log(Alk)</u>	<u>log(SC)</u>	<u>log(Q)</u>	<u>Regression</u>	<u>Computed Alk</u>	<u>Residual log(Alk)</u>	<u>Normal Quantiles</u>
5/1/1998	868	729	140	2.15	2.94	2.86	174	-0.095	-1.37	
5/6/1998	803	143	202	2.31	2.16	194	0.018	0.248		
5/11/1998	911	128	240	2.38	2.96	2.11	215	0.048	0.734	
5/14/1998	322	1947	52.0	1.72	2.51	3.29	76.5	-0.168	-2.13	
5/27/1998	844	100	228	2.36	2.93	2.00	208	0.039	0.634	
6/16/1998	877	43.5	236	2.37	2.94	1.64	233	0.005	0.055	
6/24/1998	598	413	121	2.08	2.78	2.62	141	-0.065	-1.10	
7/13/1998	316	243	78.0	1.89	2.50	2.39	93.0	-0.076	-1.22	
7/20/1998	558	44.8	180	2.26	2.75	1.65	167	0.033	0.468	
8/6/1998	819	28.7	224	2.35	2.91	1.46	231	-0.014	-0.381	
9/15/1998	877	14.5	254	2.41	2.94	1.16	260	-0.010	-0.281	
9/22/1998	201	913	57.0	1.76	2.30	2.96	58.5	-0.011	-0.331	
9/25/1998	88.0	6590	32.0	1.51	1.94	3.82	26.2	0.086	1.41	
10/5/1998	108	7490	36.0	1.56	2.03	3.87	30.1	0.078	1.33	
10/22/1998	425	104	106	2.03	2.63	2.02	126	-0.074	-1.19	
11/5/1998	200	8776	37.0	1.57	2.30	3.94	46.4	-0.099	-1.45	
12/4/1998	729	222	190	2.28	2.86	2.35	173	0.041	0.654	
1/12/1999	1101	113	284	2.45	3.04	2.05	250	0.055	0.889	
2/1/1999	306	4676	52.0	1.72	2.49	3.67	67.5	-0.113	-1.73	
2/19/1999	1041	119	267	2.43	3.02	2.08	239	0.049	0.777	
3/16/1999	1337	110	256	2.41	3.13	2.04	289	-0.052	-0.820	

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9/24/2009	246	333	67.0	1.83	2.39	2.52	75.0	-0.049	-0.798
11/3/2009	327	328	85.0	1.93	2.52	2.52	92.5	-0.037	-0.634
11/19/2009	780	65.0	249	2.40	2.89	1.81	206	0.083	1.37
12/1/2009	921	54.7	273	2.44	2.96	1.74	236	0.063	1.07
12/17/2009	1030	58.7	284	2.45	3.01	1.77	254	0.048	0.755
1/6/2010	1150	94.5	302	2.48	3.06	1.98	263	0.060	1.01
1/19/2010	1040	79.7	296	2.47	3.02	1.90	248	0.076	1.29
2/4/2010	949	63.9	250	2.40	2.98	1.81	238	0.022	0.298
2/23/2010	997	69.3	244	2.39	3.00	1.84	244	0.000	-0.119
3/10/2010	712	547	212	2.33	2.85	2.74	155	0.135	2.32
4/14/2010	1040	52.7	295	2.47	3.02	1.72	259	0.057	0.937
4/23/2010	601	228	193	2.29	2.78	2.36	150	0.110	1.90
5/13/2010	349	544	102	2.01	2.54	2.74	92.2	0.044	0.694
6/9/2010	170	2448	42.0	1.62	2.23	3.39	46.9	-0.048	-0.777
6/10/2010	228	3345	70.0	1.85	2.36	3.52	56.3	0.095	1.66
6/13/2010	104	11316	38.0	1.58	2.02	4.05	28.1	0.132	2.13
6/14/2010	107	15162	40.0	1.60	2.03	4.18	27.8	0.158	2.67
6/15/2010	192	6480	55.0	1.74	2.28	3.81	46.5	0.073	1.22
6/16/2010	203	4806	64.0	1.81	2.31	3.68	49.9	0.108	1.81
7/6/2010	104	13387	34.0	1.53	2.02	4.13	27.6	0.091	1.55
8/19/2010	632	60.8	218	2.34	2.80	1.78	177	0.090	1.50
8/25/2010	524	770	126	2.10	2.72	2.89	120	0.022	0.281
11/16/2010	500	262	86.0	1.93	2.70	2.42	129	-0.176	-2.32
1/19/2011	1100	83.3	318	2.50	3.04	1.92	258	0.091	1.60
3/7/2011	759	50.8	232	2.37	2.88	1.71	206	0.051	0.843
3/16/2011	806	48.0	237	2.38	2.91	1.68	217	0.038	0.615
4/6/2011	957	37.6	252	2.40	2.98	1.58	252	0.000	-0.103
4/18/2011	942	32.8	268	2.43	2.97	1.52	253	0.026	0.364
5/2/2011	937	28.8	276	2.44	2.97	1.46	255	0.035	0.577
6/7/2011	691	21.9	210	2.32	2.84	1.34	210	0.000	-0.087
6/21/2011	890	110	184	2.27	2.95	2.04	215	-0.067	-1.13
6/22/2011	854	46.2	134	2.13	2.93	1.66	227	-0.229	-2.67
8/15/2011	376	25.5	104	2.02	2.58	1.41	132	-0.105	-1.60
9/22/2011	391	42.9	112	2.05	2.59	1.63	129	-0.062	-1.07