

SITE NUMBER—07144100

SITE NAME—Little Arkansas River near Sedgwick

DATE CREATED—3/18/2013

MODEL DEVELOPMENT DATA PERIOD—5/1/1998 – 9/22/2011

MODEL-CALIBRATION DATASET—All data were collected using U.S. Geological Survey (USGS) protocols and are stored in National Water Information System (NWIS) database. The regression model is based on 162 concurrent measurements of specific conductance and sodium samples collected from 05-01-1998 through 09-22-2011. Samples were collected throughout the range of continuously observed specific conductance conditions. Specific conductance values are time-averaged, approved unit values corresponding with the duration of sample collection. Summary statistics and complete model-calibration dataset are provided. No sodium values were deemed outliers.

MODEL DEVELOPMENT—Regression analysis was done using S-PLUS, R, and a spreadsheet macro that examined specific conductance as an explanatory variable for estimating sodium. Different combinations of untransformed and \log_{10} -transformed data were evaluated. Sodium and specific conductance were selected as the best model based on residual plots, model standard percentage error (*MSPE*), adjusted R^2 , prediction error sum of squares (*PRESS*), and Mallow's C_p . Model spreadsheet is archived and can be found at <http://nrtwq.usgs.gov/ks> for review, and contains all relevant sample data and more in-depth statistical information.

MODEL SUMMARY—Summary of final regression analysis for sodium concentration at site number 07144100.

Specific conductance-based model:

$$\log_{10}(Na) = 1.34 \times \log_{10}(SC) - 2.09,$$

where

Na = sodium, in milligrams per liter; and

SC = specific conductance, in microsiemens per centimeter at 25 degrees Celsius.

The use of specific conductance as an explanatory variable makes sense both physically and statistically. It makes sense physically because sodium is a major ion that affects the conductivity of water. This correlates well with specific conductance because specific conductance measures the conductivity of water. Specific conductance makes statistical sense as an explanatory variable because it resulted in a model with low Mallow's C_p and *PRESS* values, and high adjusted R^2 values.

SODIUM RECORD— The record is computed using the regression model in the National Real-Time Water Quality (NRTWQ) website. Data are computed at hourly intervals. The record is complete for the year except as noted. The specific conductance monitor was removed during winter months because of below freezing conditions. A more in-depth description of the water quality record can be found at –

<http://nrtwq.usgs.gov/ks>

REMARKS—

- Site location, equipment, and other stream-gaging station information can be found in the Site Information Management System (SIMS).

Computed: Aaron King

Reviewed: Patrick Rasmussen

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Model Form

$\log(\text{Na}) = 1.34 * \log(\text{SC}) - 2.09$

Explanatory variable summary statistics

	log(SC)	SC
Minimum	1.732	54.0
1st Quartile	2.441	276
Median	2.773	593
Mean	2.677	585
3rd Quartile	2.941	871
Maximum	3.126	1340

Notes:

Dependent variable summary statistics

	log(Na)	Na
Minimum	0.1761	1.50
1st Quartile	1.207	16.1
Median	1.626	42.3
Mean	1.496	44.5
3rd Quartile	1.845	70.0
Maximum	2.121	132

Notes:

Model Calibration

Basic Data

Number of Measurements:	162
Standard Error:	0.06333
MSPE (Upper)	+15.7
MSPE (Lower)	-13.57
R ²	0.98
Adj R ²	0.98
Duan BCF:	1.01

Explanatory Variables

Variable	Value	Standard Error
Intercept	-2.09	0.0439
log(SC)	1.34	0.0163

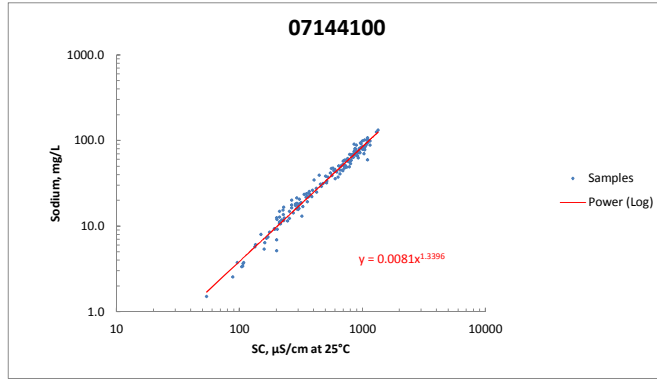
Notes:

Covariance Matrix

	Intercept	log(SC)
Intercept	1	-0.994
log(SC)	-0.994	1

Test Criteria

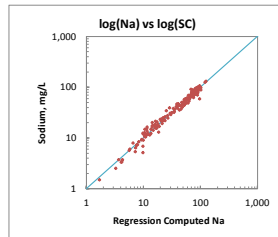
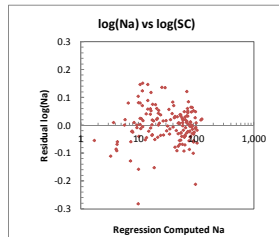
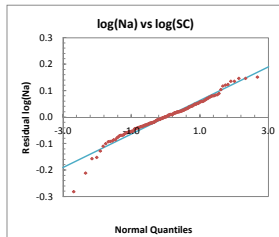
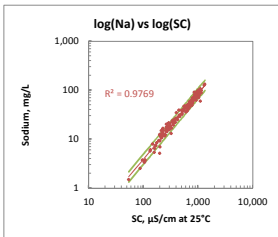
	Leverage	Cook's D	DFITS
	0.0370	0.792	0.222



Observations exceeding at least one test criterion

Observation	Observed log(Na)	Predicted log(Na)	Residuals	Standardized Residuals	Studentized Residuals	Leverage	Cook's D	DFITS
4	1.12	1.27	-0.153	-2.43	-2.47	0.00805	0.0239	-0.222
13	0.838	0.996	-0.157	-2.50	-2.55	0.0154	0.0491	-0.319
14	0.405	0.515	-0.110	-1.77	-1.79	0.0417	0.0684	-0.372
17	0.711	0.993	-0.282	-4.49	-4.78	0.0155	0.158	-0.600
33	1.17	1.03	0.147	2.33	2.36	0.0143	0.0394	0.285
44	1.22	1.07	0.151	2.39	2.43	0.0129	0.0374	0.278
52	0.575	0.566	0.00950	0.153	0.153	0.0381	0.000463	0.0303
65	1.19	1.06	0.124	1.97	1.99	0.0131	0.0257	0.229
84	1.30	1.16	0.147	2.33	2.36	0.0104	0.0285	0.242
94	0.176	0.231	-0.0547	-0.894	-0.893	0.0652	0.0278	-0.236
127	0.732	0.859	-0.127	-2.03	-2.05	0.0211	0.0446	-0.302
144	0.533	0.623	-0.0905	-1.45	-1.46	0.0342	0.0375	-0.275
148	0.526	0.613	-0.0863	-1.39	-1.39	0.0349	0.0348	-0.265
152	1.77	1.98	-0.211	-3.36	-3.47	0.0149	0.0855	-0.428

Notes:



Date	SC, µS/cm at 25°C	Streamflow, ft ³ /sec	Sodium, mg/L	log(Na)	log(SC)	Regression Computed Na	Residual log(Na)	Normal Quantiles	90% P.L. Lower	90% P.L. Upper
5/1/1998	868	729	80.7	1.91	2.94	70.3	0.060	1.11	55.2	89.5
5/6/1998	803	143	58.3	1.77	2.91	63.3	-0.036	-0.713	49.7	80.6
5/11/1998	911	128	66.0	1.82	2.96	75.0	-0.055	-1.06	58.9	95.5
5/14/1998	322	1947	13.1	1.12	2.51	18.6	-0.153	-2.01	14.6	23.7
5/27/1998	844	100	63.5	1.80	2.93	67.7	-0.028	-0.543	53.2	86.2
6/16/1998	877	43.5	67.6	1.83	2.94	71.3	-0.023	-0.439	56.0	90.7
6/24/1998	598	413	45.9	1.66	2.78	42.7	0.032	0.598	33.5	54.3
7/10/1998	211	1360	11.2	1.05	2.32	10.6	0.025	0.508	8.3	13.5
7/13/1998	316	243	18.8	1.27	2.50	18.2	0.015	0.258	14.3	23.1
7/20/1998	558	44.8	47.1	1.67	2.75	38.9	0.083	1.47	30.6	49.5
8/6/1998	819	28.7	63.7	1.80	2.91	65.0	-0.009	-0.194	51.1	82.8
9/15/1998	877	14.5	80.2	1.90	2.94	71.3	0.051	0.906	56.0	90.7
9/22/1998	201	913	6.89	0.838	2.30	9.90	-0.158	-2.14	7.8	12.6
9/25/1998	88.0	6590	2.54	0.405	1.94	3.28	-0.110	-1.82	2.6	4.2
10/5/1998	108	7490	3.76	0.575	2.03	4.31	-0.059	-1.14	3.4	5.5
10/22/1998	425	104	24.9	1.40	2.63	27.0	-0.035	-0.674	21.2	34.4
11/5/1998	200	8776	5.14	0.711	2.30	9.84	-0.282	-2.68	7.7	12.5
12/4/1998	729	222	50.8	1.71	2.86	55.6	-0.039	-0.795	43.7	70.8
1/12/1999	1101	113	94.4	1.98	3.04	96.7	-0.010	-0.226	75.9	123.0
2/1/1999	306	4676	20.7	1.32	2.49	17.4	0.076	1.30	13.7	22.1
2/19/1999	1041	119	78.9	1.90	3.02	89.7	-0.056	-1.08	70.4	114.1
3/16/1999	1337	110	132	2.12	3.13	125	0.022	0.439	98.5	159.6
3/23/1999	1095	98.1	102	2.01	3.04	95.9	0.027	0.526	75.4	122.1
4/7/1999	404	1651	34.5	1.54	2.61	25.2	0.136	2.01	19.8	32.5
4/16/1999	200	5410	12.5	1.10	2.30	9.84	0.104	1.62	7.7	12.5
5/5/1999	802	239	53.8	1.73	2.90	63.2	-0.070	-1.34	49.7	80.5
5/24/1999	211	1664	12.7	1.10	2.32	10.6	0.080	1.34	8.3	13.5
6/18/1999	300	410	17.0	1.23	2.48	16.9	0.002	0.023	13.3	21.5
6/21/1999	220	2223	11.8	1.07	2.34	11.2	0.024	0.473	8.8	14.2
7/20/1999	176	3521	8.47	0.928	2.25	8.29	0.009	0.163	6.5	10.5
8/3/1999	149	4238	7.97	0.902	2.17	6.63	0.080	1.38	5.2	8.4

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5/13/2010	349	544	23.8	1.38	2.54	20.7	0.060	1.08	16.3	26.4
6/9/2010	170	2448	7.47	0.873	2.23	7.91	-0.025	-0.490	6.2	10.1
6/10/2010	228	3345	11.6	1.06	2.36	11.7	-0.005	-0.132	9.2	14.9
6/13/2010	106	7905	3.41	0.533	2.03	4.20	-0.091	-1.56	3.3	5.3
6/14/2010	107	15162	3.64	0.561	2.03	4.26	-0.068	-1.24	3.3	5.4
6/15/2010	192	6480	9.32	0.969	2.28	9.31	0.000	-0.039	7.3	11.9
6/16/2010	203	4806	9.17	0.962	2.31	10.0	-0.039	-0.774	7.9	12.8
7/6/2010	104	13387	3.36	0.526	2.02	4.10	-0.086	-1.47	3.2	5.2
8/19/2010	632	60.8	37.2	1.57	2.80	46.0	-0.092	-1.62	36.1	58.5
8/25/2010	524	770	37.4	1.57	2.72	35.8	0.020	0.372	28.1	45.5
11/16/2010	500	262	38.3	1.58	2.70	33.6	0.057	1.00	26.4	42.7
1/19/2011	1100	83.3	59.3	1.77	3.04	96.5	-0.212	-2.33	75.8	122.9
3/7/2011	759	50.8	61.4	1.79	2.88	58.7	0.019	0.355	46.1	74.7
3/16/2011	806	48.0	68.1	1.83	2.91	63.6	0.029	0.561	50.0	81.0
4/6/2011	957	37.6	82.1	1.91	2.98	80.1	0.011	0.210	62.9	102.0
4/18/2011	942	32.8	80.6	1.91	2.97	78.4	0.012	0.226	61.6	99.8
5/2/2011	937	28.8	77.1	1.89	2.97	77.9	-0.004	-0.101	61.2	99.1
6/7/2011	691	21.9	52.5	1.72	2.84	51.8	0.006	0.070	40.7	65.9
6/21/2011	890	110	88.3	1.95	2.95	72.7	0.085	1.51	57.1	92.5
6/22/2011	854	46.2	90.9	1.96	2.93	68.8	0.121	1.74	54.0	87.5
8/15/2011	376	25.5	23.3	1.37	2.58	22.9	0.007	0.101	18.0	29.2
9/22/2011	391	42.9	26.3	1.42	2.59	24.2	0.037	0.674	19.0	30.7