Model Archive Summary for Suspended Sediment Concentration at Station 01480617; West Branch Brandywine Creek at Modena, Pennsylvania [2020 Version]

This model archive summary describes the regression model developed to estimate continuous instantaneous (15-minute) suspended sediment concentrations starting in 2007. The model was updated in June 2020, using all available calibration data. The previous model (Sloto and Olsen, 2011) was in use from October 1, 2008 to September 30, 2019. The new model is used to compute suspended sediment concentrations beginning in October 2019.

Site and Model Information

U.S. Geological Survey (USGS) station number: 01480617

Station name: West Branch Brandywine Creek at Modena, Pennsylvania

Lat 39°57'42", long 75°48'06" referenced to North American Datum of 1927, Chester County, PA, Hydrologic Unit 02040205, on left bank at bridge on SR 15068 at Modena, and 300 ft upstream from Dennis Run.

Date regression model was created: June 2020.

Period of data for model calibration: November 16, 2007 – March 22, 2019.

Model application date: October 2019 onward.

Database Reviewed by: Elizabeth A. Hillte, May 2020

Computed by: Matthew C. Gyves, June 2020.

Approved by: Joseph W. Duris, Water-Quality Specialist, June 2020.

Equipment

A Yellow Spring Instrument (YSI) 6920V2 monitor equipped with sensors for temperature, specific conductance, pH, dissolved oxygen, and turbidity (6136 sensor) is deployed at this site. The monitor is housed in a 4-inch perforated plastic pipe placed in the stream about 3 ft from the left bank. Readings from the sensors are recorded every 15 minutes and transmitted hourly by way of GOES satellite.

Model Calibration Dataset

All data were collected using standard USGS protocols and are stored in the National Water Information System (NWIS) database. Linear regression models were developed using RStudio Version 1.2.1335. Primary packages included (dataRetrieval, v 2.7.5; dplyr, v 0.8.3, plotly, v 4.9.0, and the Model Archive Summary Shiny App (available at https://github.com/PatrickEslick/ModelArchiveSummary). Explanatory variables evaluated as inputs to linear regression were turbidity and streamflow.

The final regression model is based on 95 concurrent measurements of suspended sediment and turbidity concentrations. Suspended sediment concentrations were determined from analysis of discrete samples, and turbidity concentrations were determined from continuous record of 15-minute values, interpolated when necessary to correspond with collection time of the discrete sample for sediment analysis. Suspended sediment samples were collected over a range of hydrologic conditions throughout each year during sampling period. Studentized residuals for final model were inspected and considered for potential removal as outliers if residual values were greater than 3 or less than -3. Although several samples met these criteria; other regression

diagnostics show their influence on model performance to be minimal, and no samples were removed from the dataset.

Prior Model

This model supersedes the prior model that was originally published in Sloto and Olsen (2011).

SSC = 1.9879 Turb - 9.6239 (October 1, 2008 to September 30, 2019)

Data Collection

Discrete samples for suspended sediment analysis were collected using an ISCO automatic sampler which was set to sample based on stage and turbidity thresholds to provide data for a broad range of turbidity values. Over time, these thresholds were changed to collect samples under different conditions, covering the range of measured values. Water was pulled by the sampler peristaltic pump through 0.5-inch tubing from an intake located near the turbidity probe and stored in 1-liter polypropylene bottles. Once collected, sample times were recorded in the field during bottle retrieval as reported by the ISCO. Samples were analyzed for suspended sediment concentration (SSC) in the laboratory at the USGS office in Exton, Pennsylvania and the USGS Kentucky Sediment Laboratory in Louisville, Kentucky using standard USGS methods. Suspended sediment concentrations ranged from 24 to 2,800 mg/L in the 95 analyzed samples.

Turbidity data were collected according to USGS Techniques and Methods 1-D3 (Wagner and Others, 2006). Turbidity concentrations ranged from 14 to 560 formazin nephelometric units (FNU) during collection of concurrent discrete suspended sediment samples used for model calibration.

Model Development

Regression analysis was done using R by examining turbidity (Turb) and streamflow (Q) as explanatory variables for SSC. A variety of linear regression models that predict SSC and $\log_{10}(SSC)$ were evaluated and computed using methods described by Rasmussen and others, 2011.

The model with $log_{10}(Turb)$ as the explanatory variable was selected as the best predictor of $log_{10}(SSC)$ on the basis of residual plots, maximizing adjusted coefficient of determination (adjusted R^2), and minimizing model residual standard error (or root mean square error, RMSE) and standard percentage error (MSPE). The addition of discharge as a variable showed minimal improvement on model performance.

Model Summary

Final regression model for suspended sediment concentration (SSC) at site number 01480617:

$$\log_{10} SSC = 0.958 \log_{10} Turb + 0.349$$

where

SSC = suspended sediment concentration in milligrams per liter (mg/L) (parameter 80154); Turb = turbidity in formazin nephelometric units (FNU) (parameter 63680);

Turb makes physical and statistical sense as explanatory variable for *SSC* because previous studies showed suspended sediment concentrations were directly related to turbidity concentrations. The transformed model may be retransformed to the original units so that SSC concentrations can be calculated directly. A potential bias that is introduced because of retransformation can be corrected using Duan's bias correction factor (BCF). For this model the BCF is 1.08. The retransformed model, using the BCF, is:

$$SSC = 2.412 \, Turb^{.958}$$

References

Rasmussen, P.P., Gray, J.R., Glysson, G.D., and Ziegler, A.C., 2009, revised 2011, Guidelines and procedures for computing time-series suspended-sediment concentrations and loads from in-stream turbidity-sensor and streamflow data: U.S. Geological Survey Techniques and Methods, book 3, chap. C4, 52 p.

Sloto, R.A., and Olson, L.E., Estimated suspended-sediment loads and yields in the French and Brandywine Creek Basins, Chester County, Pennsylvania, water years 2008–09: U.S. Geological Survey Scientific Investigations Report 2011–5109, 31 p.

Wagner, R.J., Boulger, R.W., Jr., Oblinger, C.J., and Smith, B.A., 2006, Guidelines and standard procedures for continuous water-quality monitors—Station operation, record computation, and data reporting: U.S. Geological Survey Techniques and Methods 1–D3, 51 p. + 8 attachments; accessed April 10, 2006, at http://pubs.water.usgs.gov/tm1d3

Model Statistics, Data, and Plots

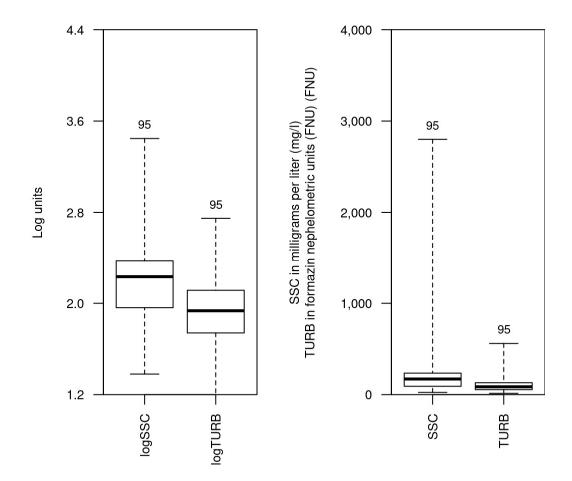
Model

logSSC = + 0.958 * logTURB + 0.349

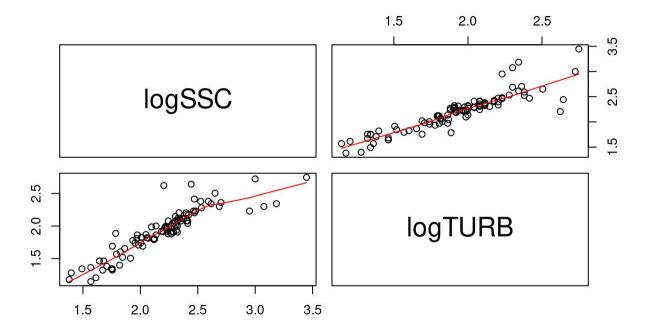
Variable Summary Statistics

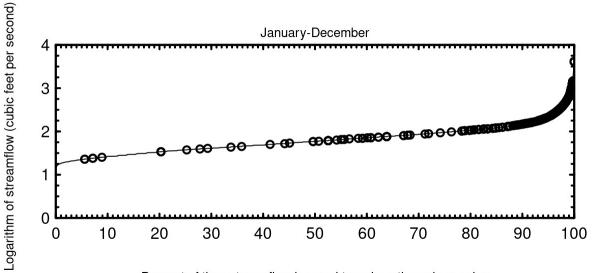
	logSSC	SSC	logTURB	TURB
Minimum	1.38	24	1.15	14
1st Quartile	1.95	90	1.74	55
Median	2.23	171	1.93	86
Mean	2.19	238	1.92	114
3rd Quartile	2.38	240	2.11	130
Maximum	3.45	2800	2.75	560

Box Plots

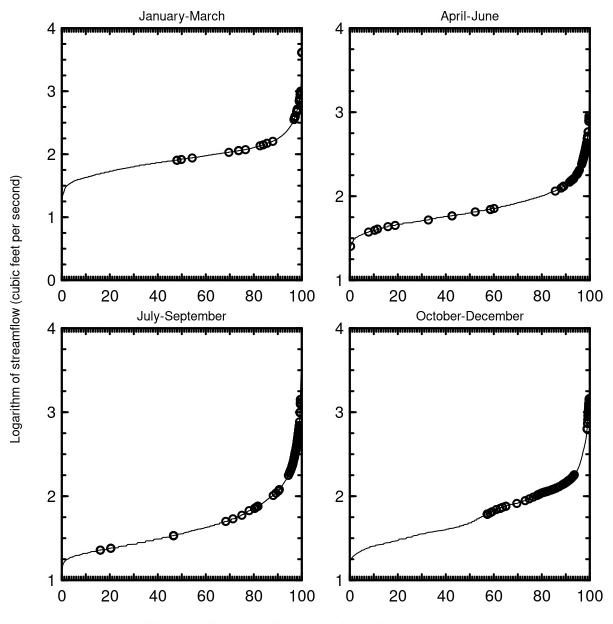


Exploratory Plots





Percent of time streamflow is equal to or less than given value



Percent of time streamflow is equal to or less than given value

Basic Model Statistics

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Number of Observations 95

Standard error (RMSE) 0.163

Average Model standard percentage error (MSPE) 38.4

Coefficient of determination (R<sup>2</sup>) 0.814

Adjusted Coefficient of Determination (Adj. R<sup>2</sup>) 0.812

Bias Correction Factor (BCF) 1.08
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Explanatory Variables

```
Coefficients Standard Error t value Pr(>|t|)
(Intercept) 0.349 0.0928 3.77 2.90e-04
logTURB 0.958 0.0476 20.10 1.11e-35
```

Correlation Matrix

```
Intercept E.vars

Intercept 1.000 -0.984

E.vars -0.984 1.000
```

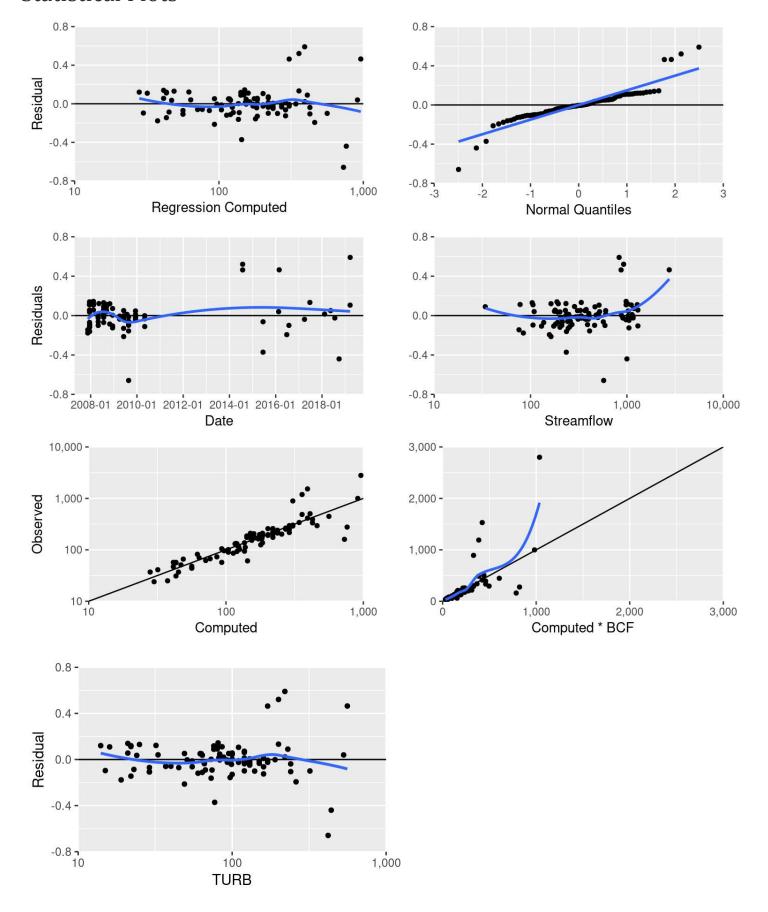
Outlier Test Criteria

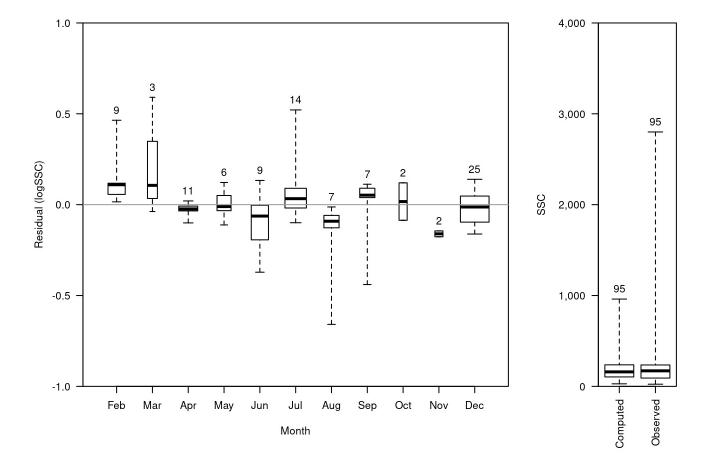
```
Leverage Cook's D DFFITS
0.0632 0.1944 0.2902
```

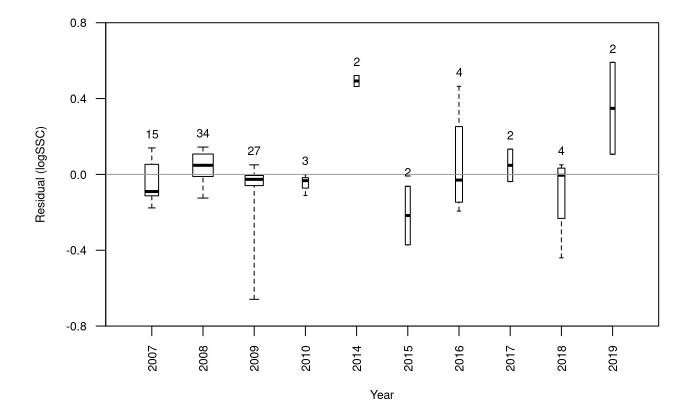
Flagged Observations

	logSSC	Estimate	Residual	Standard Residual	Studentized Residual	Leverage	Cook's D	DFFITS
2009-08-22 00:0	0 2.20	2.86	-0.6590	-4.160	-4.580	0.0529	0.48300	-1.0800
2014-07-28 11:0	0 3.08	2.55	0.5210	3.240	3.420	0.0230	0.12400	0.5250
2014-07-28 11:3	0 2.95	2.49	0.4640	2.880	3.000	0.0188	0.07940	0.4150
2016-02-16 13:0	0 3.00	2.96	0.0398	0.253	0.252	0.0660	0.00226	0.0669
2016-02-25 05:0	0 3.45	2.98	0.4650	2.960	3.090	0.0693	0.32500	0.8430
2018-09-28 11:4	5 2.44	2.88	-0.4400	-2.780	-2.890	0.0554	0.22600	-0.6990
2019-03-22 01:0	0 3.18	2.59	0.5910	3.680	3.950	0.0259	0.17900	0.6450

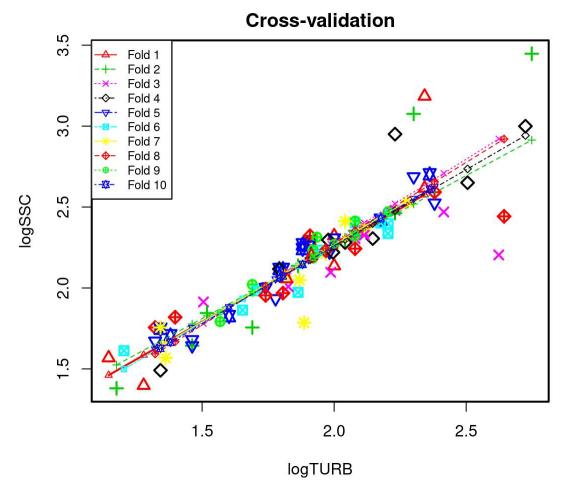
Statistical Plots







Cross Validation



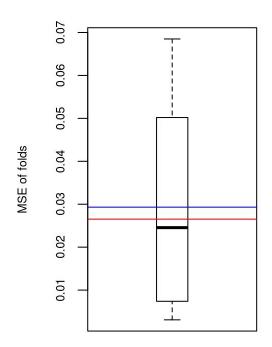
```
Minimum MSE of folds: 0.00307

Mean MSE of folds: 0.02930

Median MSE of folds: 0.02460

Maximum MSE of folds: 0.06850

(Mean MSE of folds) / (Model MSE): 1.11000
```



Red line - Model MSE

Blue line - Mean MSE of folds

Model-Calibration Data Set

	Date	logSSC	logTURB	SSC	TURB	Computed	Computed	Residual	Normal	Censored
0						logSSC	SSC		Quantiles	Values
1	2007-11-16	1.4	1.28	25	19	1.57	40.5	-0.177	-1.56	
2	2007-11-16	1.49	1.34	31	22	1.64	46.6	-0.144	-1.34	
3	2007-12-13	1.61	1.2	41	16	1.5	34.3	0.11	0.979	
4	2007-12-14	1.57	1.15	37	14	1.45	30.2	0.121	1.28	
5	2007-12-14	1.67	1.32	47	21	1.62	44.6	0.0558	0.648	
6	2007-12-14	1.71	1.38	51	24	1.67	50.6	0.0357	0.321	
7	2007-12-14	1.68	1.46	48	29	1.75	60.7	-0.0694	-0.648	
8	2007-12-14	1.76	1.32	57	21	1.62	44.6	0.14	1.56	
9	2007-12-14	1.64	1.46	44	29	1.75	60.7	-0.107	-1.07	
10	2007-12-16	1.38	1.18	24	15	1.48	32.3	-0.0961	-0.821	
11	2007-12-16	1.64	1.46	44	29	1.75	60.7	-0.107	-1.02	

:	12 2007-12-16	1.93	1.78	86	60	2.05	122	-0.119	-1.17	
	13 2007-12-16	1.97	1.86	94	73	2.13	147	-0.162	-1.48	
:	14 2007-12-16	2.01	1.83	102	67	2.1	135	-0.0905	-0.749	
:	15 2007-12-16	2.12	1.8	133	63	2.07	128	0.0504	0.493	
:	16 2008-02-13	2.32	1.91	210	81	2.18	162	0.144	1.66	
:	17 2008-02-13	2.29	1.91	194	81	2.18	162	0.11	1.02	
:	18 2008-02-13	2.27	1.88	186	76	2.15	153	0.118	1.17	
:	19 2008-02-13	2.29	1.91	193	81	2.18	162	0.107	0.937	
:	20 2008-02-13	2.31	1.93	206	86	2.2	172	0.111	1.07	
:	21 2008-02-13	2.32	2	210	100	2.27	199	0.0565	0.681	
	22 2008-04-28	2.21	1.97	163	93	2.24	185	-0.0234	-0.212	
:	23 2008-04-29	2.38	2.11	240	130	2.37	256	0.00529	0.159	
2	24 2008-04-29	2.29	2.04	197	110	2.31	218	-0.0109	-0.0527	
2	25 2008-04-29	2.23	1.94	171	88	2.21	176	0.0204	0.266	
	26 2008-04-29	2.31	2.15	202	140	2.41	274	-0.1	-0.937	
	27 2008-04-29	2.4	2.2	250	160	2.46	312	-0.0634	-0.616	
:	28 2008-05-09	1.91	1.51	82	32	1.79	66.7	0.122	1.34	
	29 2008-07-23	2.7	2.36	504	230	2.61	442	0.0901	0.821	
	30 2008-07-24	1.82	1.4	66	25	1.69	52.7	0.131	1.41	
	31 2008-07-24	2.31	2	204	100	2.27	199	0.0439	0.435	
	32 2008-07-24	2.62	2.34	413	220	2.59	423	0.0221	0.294	
	33 2008-07-24	2.4	2.08	253	120	2.34	237	0.0615	0.715	
	34 2008-07-24	2.3	1.98	198	95	2.24	189	0.0523	0.585	
	35 2008-07-24	2.14	1.86	137	73	2.13	147	0.00193	0.106	
	36 2008-07-24	2.07	1.81	117	65	2.09	132	-0.0183	-0.159	
	37 2008-07-24	1.86	1.65	73	45	1.93	92.5	-0.0701	-0.681	
	38 2008-09-06	2.24	1.88	174	76	2.15	153	0.089	0.784	
	39 2008-09-07	2.02	1.69	105	49	1.97	100	0.0523	0.616	
	40 2008-09-07	2.26	1.9	184	80	2.17	161	0.0919	0.858	
	41 2008-09-07	2.12	1.81	131	64	2.08	130	0.0372	0.349	
	42 2008-09-07	1.85	1.52	70	33	1.8	68.7	0.0407	0.406	
	43 2008-09-07	1.75	1.34	56	22	1.64	46.6	0.113	1.12	
	44 2008-10-28	1.57	1.36	37	23	1.65	48.6	-0.086	-0.715	
	45 2008-10-29	1.76	1.34	57	22	1.64	46.6	0.12	1.22	
	46 2008-12-12	2.53	2.38	335	240	2.63	460	-0.105	-0.979	
	47 2008-12-12	2.41	2.08	259	120	2.34	237	0.0717	0.749	
	48 2008-12-12	2.34	2.2	217	160	2.46	312	-0.125	-1.22	
	49 2008-12-12	2.27	2	186	100	2.27	199	0.00376	0.132	

50	2009-04-03	2.34	2.11	220	130	2.37	256	-0.0325	-0.321	
5:	1 2009-04-03	2.36	2.11	231	130	2.37	256	-0.0113	-0.0791	
52	2 2009-04-03	2.31	2.08	202	120	2.34	237	-0.0363	-0.406	
53	3 2009-04-04	2.22	1.98	167	96	2.25	191	-0.026	-0.294	
5	4 2009-04-04	2.23	1.97	170	93	2.24	185	-0.0051	0	
5.	5 2009-05-07	2.32	2.08	210	120	2.34	237	-0.0194	-0.185	
5	6 2009-06-04	2.14	2	137	100	2.27	199	-0.129	-1.28	
5	7 2009-06-05	1.76	1.69	57	49	1.97	100	-0.213	-1.78	
58	3 2009-06-05	1.98	1.71	96	51	1.99	104	-0.00328	0.0527	
5 !	9 2009-06-05	2.12	1.79	131	62	2.07	126	0.0504	0.523	
60	2009-06-06	2.06	1.82	114	66	2.09	134	-0.0359	-0.377	
63	1 2009-07-28	2.35	2.08	226	120	2.34	237	0.0125	0.212	
62	2 2009-08-22	2.2	2.62	160	420	2.86	786	-0.659	-2.49	
63	3 2009-08-22	2.24	2.08	175	120	2.34	237	-0.0986	-0.858	
6	1 2009-08-22	2.1	1.99	125	97	2.25	193	-0.156	-1.41	
6.5	5 2009-08-22	2.05	1.87	112	74	2.14	149	-0.0912	-0.784	
6	6 2009-08-22	2	1.74	101	55	2.02	112	-0.0127	-0.106	
6	7 2009-08-22	1.83	1.6	67	40	1.88	82.6	-0.0584	-0.523	
68	3 2009-08-22	1.79	1.57	62	37	1.85	76.7	-0.0596	-0.554	
6	9 2009-12-09	2.18	1.92	153	83	2.19	166	-0.00352	0.0263	
7 (2009-12-09	2.24	1.92	172	83	2.19	166	0.0473	0.464	
7:	1 2009-12-09	2.22	2	166	99	2.26	197	-0.0415	-0.464	
72	2 2009-12-09	2.33	2.11	212	130	2.37	256	-0.0486	-0.493	
7:	3 2009-12-09	2.42	2.18	264	150	2.43	293	-0.0129	-0.132	
7	4 2009-12-09	2.48	2.23	302	170	2.49	331	-0.00655	-0.0263	
7:	5 2009-12-09	2.46	2.23	290	170	2.49	331	-0.0242	-0.239	
7 (5 2009-12-09	2.47	2.2	296	160	2.46	312	0.00996	0.185	
7	7 2010-05-03	2.53	2.28	340	190	2.53	368	-0.00136	0.0791	
78	3 2010-05-03	2.4	2.18	252	150	2.43	293	-0.0331	-0.349	
7 :	9 2010-05-04	1.97	1.81	93	64	2.08	130	-0.112	-1.12	
8 (2014-07-28	3.08	2.3	1190	200	2.55	386	0.521	2.12	
8:	1 2014-07-28	2.95	2.23	892	170	2.49	331	0.464	1.78	
82	2 2015-06-15	1.95	1.74	90	55	2.02	112	-0.0627	-0.585	
83	3 2015-06-15	1.79	1.89	61	77	2.16	155	-0.372	-1.92	
8	4 2016-02-16	3	2.72	999	530	2.96	983	0.0398	0.377	
8 !	5 2016-02-25	3.45	2.75	2800	560	2.98	1040	0.465	1.92	
8	5 2016-06-24	2.47	2.41	295	260	2.66	497	-0.194	-1.66	
8.	7 2016-07-28	2.65	2.51	447	320	2.75	606	-0.0995	-0.897	

2.59	2.38 39	1 240	2.63	460	-0.0379	-0.435	
2.69	2.3 48	7 200	2.55	386	0.133	1.48	
2.2	1.91 15	8 82	2.18	164	0.0155	0.239	
2.12	1.79 13	1 62	2.07	126	0.0504	0.554	
2.28	2.04 19	1 110	2.31	218	-0.0244	-0.266	
2.44	2.64 27	7 440	2.88	822	-0.44	-2.12	
2.41	2.04 25	8 110	2.31	218	0.106	0.897	
3.18	2.34 153	0 220	2.59	423	0.591	2.49	
	2.69 2.2 2.12 2.28 2.44 2.41	2.69 2.3 48 2.2 1.91 15 2.12 1.79 13 2.28 2.04 19 2.44 2.64 27 2.41 2.04 25	2.69 2.3 487 200 2.2 1.91 158 82 2.12 1.79 131 62 2.28 2.04 191 110 2.44 2.64 277 440 2.41 2.04 258 110	2.69 2.3 487 200 2.55 2.2 1.91 158 82 2.18 2.12 1.79 131 62 2.07 2.28 2.04 191 110 2.31 2.44 2.64 277 440 2.88 2.41 2.04 258 110 2.31	2.69 2.3 487 200 2.55 386 2.2 1.91 158 82 2.18 164 2.12 1.79 131 62 2.07 126 2.28 2.04 191 110 2.31 218 2.44 2.64 277 440 2.88 822 2.41 2.04 258 110 2.31 218	2.69 2.3 487 200 2.55 386 0.133 2.2 1.91 158 82 2.18 164 0.0155 2.12 1.79 131 62 2.07 126 0.0504 2.28 2.04 191 110 2.31 218 -0.0244 2.44 2.64 277 440 2.88 822 -0.44 2.41 2.04 258 110 2.31 218 0.106	2.69 2.3 487 200 2.55 386 0.133 1.48 2.2 1.91 158 82 2.18 164 0.0155 0.239 2.12 1.79 131 62 2.07 126 0.0504 0.554 2.28 2.04 191 110 2.31 218 -0.0244 -0.266 2.44 2.64 277 440 2.88 822 -0.44 -2.12 2.41 2.04 258 110 2.31 218 0.106 0.897

Definitions

SSC: Suspended sediment concentration (SSC) in mg/1 (80154)

TURB: Turbidity in FNU (63680)